

# TUTORÍA MATEMÁTICAS. Derivadas y análisis de funciones (I)

1. Calcula las siguientes derivadas:

1	$f(x)=0$	11	$f(x) = -\frac{2}{x^3} + \frac{3}{x^2} - 4x$	21	$f(x) = \frac{2\sqrt{x} + \sqrt[3]{x}}{\sqrt{x}}$
2	$f(x)=-7$	12	$f(x) = \frac{x^2-1}{(x+1)^2}$	22	$f(x) = (x^5 - x^3 + 3)^4$
3	$f(x)=-7x$	13	$f(x) = \frac{5x^4-3x^3}{x^5}$	23	$f(x) = (x^2 - 2)^2$
4	$f(x)=-5x+2$	14	$f(x) = \sqrt{x^3}$	24	$f(x) = (x-1) \cdot (x+1)^2$
5	$f(x) = x^5 - x^3 + 3$	15	$f(x) = \frac{1}{\sqrt{x^3}}$	25	$f(x) = (x^5 - x^3 + 3)^4$
6	$f(x) = 2x^7 - 3x^6 + 3x^3 - 4x^2 - 7$	16	$f(x) = \sqrt{x^3} - \sqrt[3]{x^5}$	26	$f(x) = \sqrt{(x^5 - x^3 + 3)}$
7	$f(x) = \frac{x-3}{2}$	17	$f(x) = -3\sqrt{x} - 2\sqrt[3]{x^2}$	27	$f(x) = \sqrt[5]{x^5 - x^3 + 3}$
8	$f(x) = -\frac{x^3+x-1}{2}$	18	$f(x) = -\frac{2}{3}\sqrt{x^3} - \sqrt{15x} - \sqrt[3]{x^5}$	28	$f(x) = \frac{1}{\sqrt[5]{x^5 - x^3 + 3}}$
9	$f(x) = -\frac{3}{2}x^3 + \frac{2}{5}x^2 - 4$	19	$f(x) = -\frac{3}{2}\sqrt{x^3} - 2x^5 - 5x^2$	29	$f(x) = \sqrt[3]{\frac{x^5 - x^3 + 3}{x^2}}$
10	$f(x) = \frac{3}{x^2}$	20	$f(x) = \frac{\sqrt{x}\sqrt[3]{x}}{\sqrt{x}}$		

30	$f(x) = \sqrt[5]{\frac{x^2+x}{x+1}}$	39	$f(x) = -\frac{2}{\sqrt{e^x}}$	49	$f(x) = \frac{e^{3x} + e^{x^2}}{3}$
31	$f(x) = \sqrt{\frac{x^2+2x+1}{x^2-1}}$	40	$f(x) = e^{x+1} - 3e^x + 2e^{x^3}$	50	$f(x) = \frac{7x^2}{x^3}$
32	$f(x) = \sqrt{\frac{x^2-1}{x^2-2x+1}}$	41	$f(x) = 3^{2x+1}$	51	$f(x) = \frac{e^{x^2}}{x^3}$
33	$f(x) = e^{x+1}$	42	$f(x) = 7^{x-1}$	52	$f(x) = \sqrt{\frac{7x^2}{x^3}}$
34	$f(x) = -3 \cdot e^{x+1}$	43	$f(x) = 7^{x^2-1}$	53	$f(x) = \ln(x+3)$
35	$f(x) = 7 \cdot e^{x^2+1}$	44	$f(x) = -\frac{1}{\sqrt{2x}}$	54	$f(x) = 7x + \ln(x-3)$
36	$f(x) = -3 \cdot e^{x^2+x-1}$	45	$f(x) = 2^{x+1} - 3 \cdot 5^x$	55	$f(x) = \ln(x^2 - 3x + 2)$
37	$f(x) = \sqrt{e^x}$	46	$f(x) = (2^{x+1} - 3 \cdot 5^x)^3$	56	$f(x) = \frac{1}{\ln(x-1)}$
38	$f(x) = \sqrt{3e^{x+1}}$	47	$f(x) = \sqrt{3^{x+1}}$	57	$f(x) = \ln \sqrt{\frac{x^2-1}{x^2-2x+1}}$
48		48	$f(x) = 7^{\sqrt{x+1}}$		

58	$f(x) = \ln \left( \sqrt{(x^5 - x^3 + 3)} \right)$	68	$f(x) = \frac{1}{\sin(x+1)}$	77	$f(x) = -\tan(-5x^2 - 7)$
59	$f(x) = \ln \left( \frac{e^x - 1}{e^x + 1} \right)$	69	$f(x) = \frac{1}{\cos x} + \frac{1}{\sin(x+1)}$	78	$f(x) = \frac{1}{\tan(x-5)}$
60	$f(x) = \log_3(x+2)$	70	$f(x) = \frac{1}{\sin x} - \frac{1}{\cos(x-1)}$	79	$f(x) = -\frac{3}{\tan(x+2)}$
61	$f(x) = \log(x-3)^2$	71	$f(x) = \sqrt[3]{\cos(3x+3)}$	80	$f(x) = \sqrt{\tan(x-5)}$
62	$f(x) = \sin(x+1)$	72	$f(x) = \frac{1}{\sin(x+1)} + (x^5 - x^3 + 3)^4$	81	$f(x) = \arcsin(x^2 - 3)$
63	$f(x) = \sin(2x^3 + 2x^2)^2$	73	$f(x) = \ln(x-1) + e^{x+1}$	82	$f(x) = 3x + \arcsin(3x^3 + 3x - 7)$
64	$f(x) = \sin(x+1) + 5x$	74	$f(x) = e^{x-3} + \cos(x+1) - x^2$	83	$f(x) = \arcsin \sqrt{(x^2 - 3)}$
65	$f(x) = \sqrt{\sin(x+1)}$	75	$f(x) = \tan(x-5)$	84	$f(x) = \arcsin \left( \frac{x+1}{x-1} \right)$
66	$f(x) = \cos(3x+3)$	76	$f(x) = \tan(x^3 + 3)$	85	$f(x) = \sqrt[3]{\sin(x^2 + 3)}$
67	$f(x) = \cos(3x^2 + 3x)$			86	$f(x) = \sqrt[3]{\tan e^x}$
				87	$f(x) = x^2 \cdot \tan \sqrt{x}$

88	$f(x) = \frac{1 + \sin^2 x}{x}$		
89	$f(x) = \ln(\sin x)$		
90	$f(x) = \arctg(x^2 - 3)$		
91	$f(x) = e^{x^2} - 3 \ln(\sin x)$	97	$f(x) = \sec x - e^x$
92	$f(x) = e^{x+3} + \ln(x - 5) - \cot(x)$	98	$f(x) = \operatorname{cosec} x + \frac{x^3}{3}$
93	$f(x) = \arctg(\ln x)$	99	$f(x) = \cot(x+1)$
94	$f(x) = \ln(\ln x)$	100	$f(x) = e^{x^2} - \cot(x^3 - 1)$
95	$f(x) = \ln(\ln x) + \arctg(x^3 - 1)$		
96	$f(x) = \cot(x^3 - 1)$		

2. Realiza un análisis completo de las siguientes funciones:

a.  $f(x) = \frac{x^2 + 1}{x}$ .

b.  $f(x) = \frac{1}{x^2 - 1}$ .

c.  $f(x) = \frac{3x}{x^2 + 1}$ .

d.  $f(x) = x\sqrt{4 - x^2}$ .

e.  $f(x) = (x - 2)e^x$ .

f.  $f(x) = xe^{-x}$ .

g.  $f(x) = \frac{e^x}{x}$ .

h.  $f(x) = \ln(x^2)$ .

i.  $f(x) = \ln(1 - x^2)$ .

j.  $f(x) = \operatorname{sen}x \operatorname{cos}x$ .